

Appendix

A Visualizations

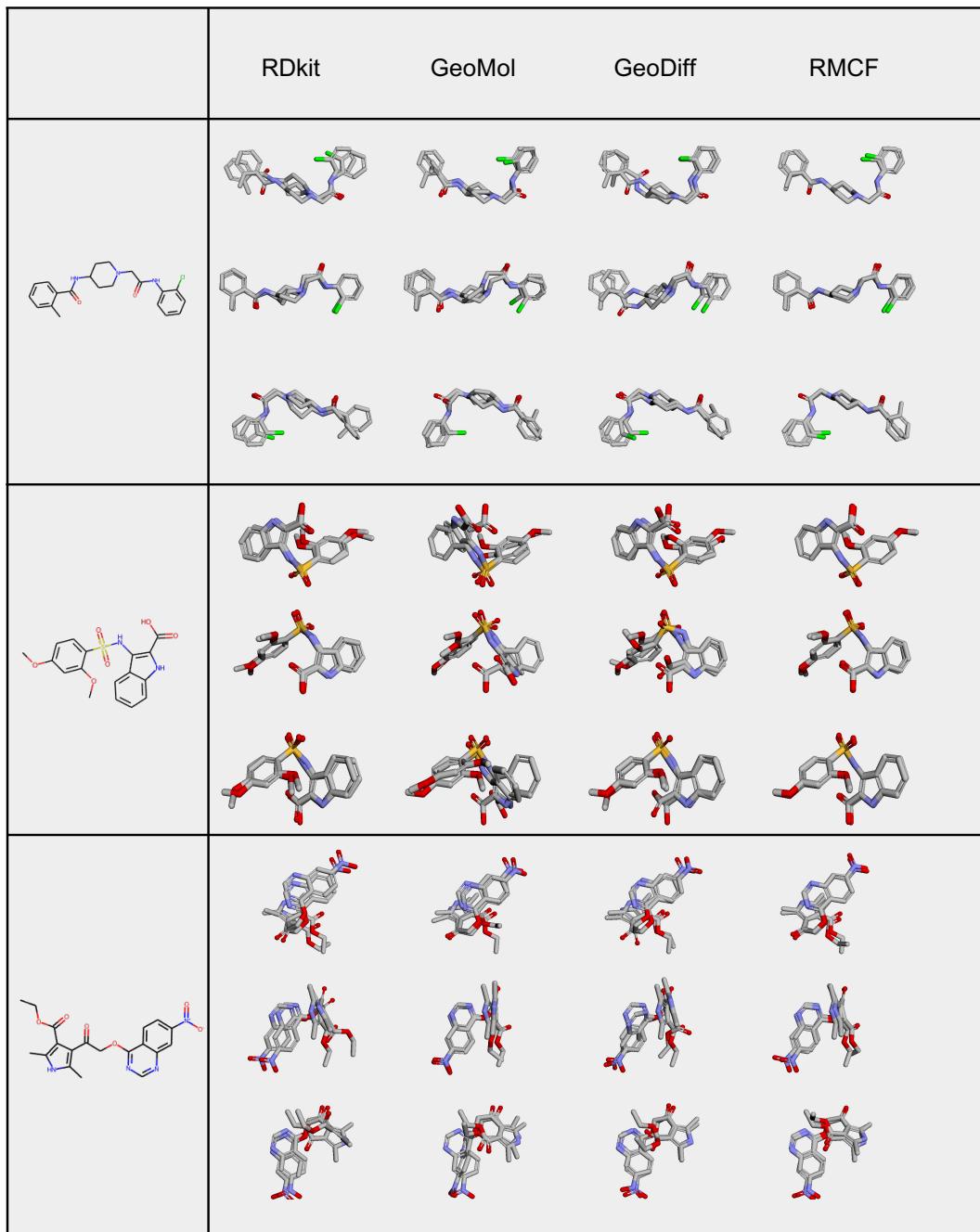


Figure 6: Examples of generated molecules from GEOM-Drugs dataset. For every model and molecule, we show three ground truths and the best-aligned conformations. Our model RMCF fits best with the references.

B Graph Dynamic Programming Algorithm

Algorithm 1 Graph Dynamic Programming for Searching the Best Partition

Require: the fragments type collection \mathcal{F} , the molecular graph G_m
Ensure: the best molecular graph partition \mathcal{P}^*

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function DoF( $f$ )
    return  $\frac{1}{|\mathcal{C}_f|} \sum_{\mathcal{C}_f} \text{RMSD}(\mathcal{C}_f, \overline{\mathcal{C}_f})^2$ 
end function
function PARTITION( $G$ )
     $s \leftarrow 100, \mathcal{P} \leftarrow \{\}$ 
    for  $f \in \mathcal{F}$  do
        if IsSubstructure( $G, f$ ) then                                 $\triangleright$  Determine if  $f$  is a substructure of  $G$ 
             $s_m \leftarrow 0, z \leftarrow 1, \mathcal{P}_m \leftarrow \{f\}$ 
             $F_r \leftarrow \text{REMOVE}(G, f)$            $\triangleright$  Cut the  $f$  and split  $G$  into fragments set  $F_r$  without  $f$ 
            for  $f \in F_r$  do
                 $dof, \mathcal{P}_f \leftarrow \text{PARTITION}(f)$ 
                 $s_m \leftarrow s + dof * |\mathcal{P}_f|, z \leftarrow z + |\mathcal{P}_f|, \mathcal{P}_m \leftarrow \mathcal{P}_m \cup \mathcal{P}_f$ 
            end for
             $s_m \leftarrow s_m / z$ 
        end if
        if  $s_m < s$  then
             $s \leftarrow s_m, \mathcal{P} \leftarrow \mathcal{P}_m$ 
        end if
        if  $\mathcal{P} = \{\}$  then
            return DoF( $G$ ),  $\{G\}$ 
        end if
    end for
end function
 $dof, \mathcal{P}^* \leftarrow \text{PARTITION}(G_m)$ 
return  $\mathcal{P}^*$ 

```

C Sampling Algorithm

Algorithm 2 Sampling Molecular Conformations From RMCF

Require: an RMCF \mathcal{G} , the number of conformations N_C , the number of sampling iterations N_S
Ensure: a set S_C containing N_C conformations

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 $S \leftarrow \{\}$ 
initialize a configuration  $\mathcal{X}$  randomly
for  $i \in [1, 2, \dots, N_S]$  do
    for  $n \in F \cup D$  do
         $U \leftarrow \{u | (n, u) \in E\}$                                  $\triangleright x_u$  is fixed in this iteration
         $P \leftarrow \text{softmax} \left\{ \sum_{u \in U} \mathbf{E}_u[x_u] \mathbf{W}_{un} \mathbf{E}_n^T + \text{out}(\mathbf{h}_n) \right\}$        $\triangleright$  the value can be pre-computed
         $x_n \sim \text{Cat}(|n|, P)$ 
    end for
    add  $\mathcal{X}$  to  $S$ 
end for
compute the pairwise distance  $K$  with Eq.11
 $S_C \leftarrow \text{run clustering with } k = N_C \text{ over } S \text{ based on } K$ 
return  $S_C$ 

```

D QM9 Results

Table 3: Results on the **GEOM-QM9** dataset, without FF optimization.

Models	COV-R (%) ↑		MAT-R (Å) ↓		COV-P (%) ↑		MAT-P (Å) ↓	
	Mean	Median	Mean	Median	Mean	Median	Mean	Median
CVGAE	0.09	0.00	1.671	1.609	-	-	-	-
GraphDG	73.33	84.21	0.425	0.397	43.90	35.33	0.581	0.582
CGCF	78.05	82.48	0.422	0.390	36.49	33.57	0.662	0.643
ConfVAE	77.84	88.20	0.415	0.374	38.02	34.67	0.622	0.609
GeoMol*	71.26	72.00	0.373	0.373	-	-	-	-
ConfGF	88.49	94.31	0.267	0.269	46.43	43.41	0.522	0.512
GeoDiff	90.07	93.39	0.209	0.199	52.79	50.29	0.445	0.440
DMCG	96.34	99.53	0.207	0.200	-	-	-	-
RMCF-R	55.86	56.67	0.433	0.414	84.86	96.51	0.260	0.227
RMCF-C	76.22	85.50	0.320	0.289	83.10	91.44	0.283	0.261

* We follow the results reported by Zhu et al. [2022], Xu et al. [2022], which use the same data splits as us. GeoMol achieves higher scores in Ganea et al. [2021]’s data splits. COV-R: 91.52/100.0, MAT-R 0.225/0.193, COV-P 86.71/100.0, MAT-P 0.270/0.241

E Hyperparamters

Table 4: Hyperparameter choices of RMCF and training phase

Hyperparameters	Values
Message Passing Neural Network	
Number of MPNN Layers N	6
Dimension of Embeddings d_{embed}	320
Dimension of Hiddens d_h	320
Dimension of Feed-forward Layers d_{ff}	1280
Dropout Rate P_{drop}	0.1
Markov Random Fields Layer	
Number of States $ f $ or $ g $	72
Dimension of Hiddens \mathbb{D}	320
Training	
Batch Size	256
Learning Rate	5×10^{-4}
Max Training Steps	1.2×10^6
Optimizer	Adam
Learning Rate Scheduler	Linear

We conducted our experiments on 8 A100 GPUs and took about 80 hours to train RMCF on GEOM-Drugs.