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# Inference by Learning: Speeding-up Graphical Model Optimization via a Coarse-to-Fine Cascade of Pruning Classifiers

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## Supplemental materials

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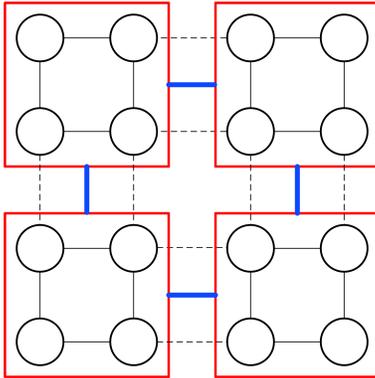
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### A Toy example for model coarsening



Given  $\mathcal{M} = (\mathcal{V}, \mathcal{E}, \mathcal{L}, \{\phi_i\}_{i \in \mathcal{V}}, \{\phi_{ij}\}_{(i,j) \in \mathcal{E}})$ , a graphical model, we create the coarsened graphical model  $\mathcal{M}' = (\mathcal{V}', \mathcal{E}', \mathcal{L}, \{\phi'_i\}_{i \in \mathcal{V}'}, \{\phi'_{ij}\}_{(i,j) \in \mathcal{E}'})$ . The vertices of  $\mathcal{V}$  are the black circles and the black thin solid and dashed lines are the edges  $\mathcal{E}$ . In this toy example, we consider a grouping function  $g$  that merges vertices of  $\mathcal{V}$  of  $2 \times 2$  subgrids together. The grouping function  $g$  creates the coarsened graphical model  $\mathcal{M}'$  where the red squares are the new induced vertices  $\mathcal{V}'$  and the solid thick blue lines are the new induced edges  $\mathcal{E}'$ .

Figure 1: Toy example for model coarsening

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## B Results

### B.1 Stereo

#### B.1.1 Tsukuba

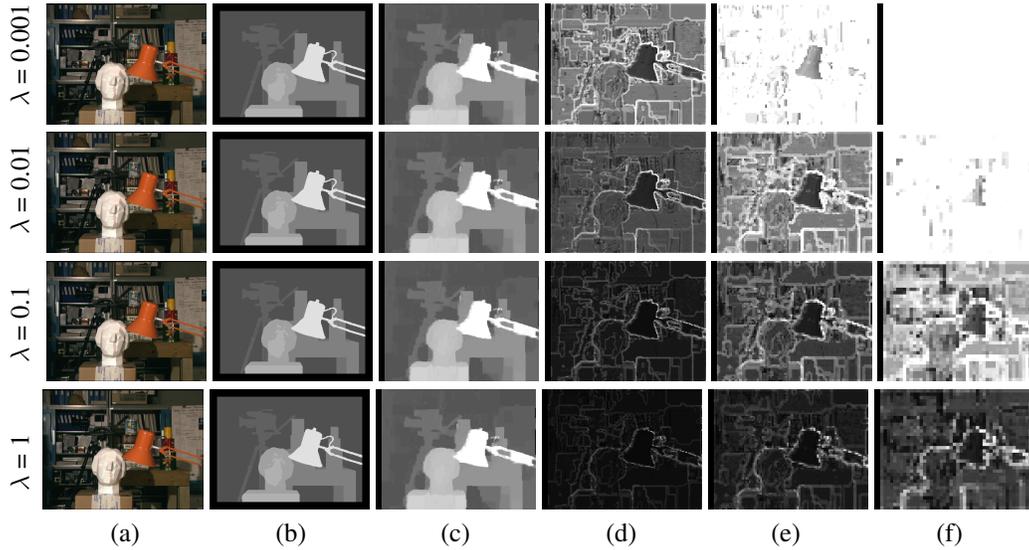


Figure 2: Results of our Inference by Learning framework for Tsukuba. Each row is a different pruning aggressiveness value ( $\lambda$ ). (a) original image, (b) ground truth, (c) solution of the pruning framework, (d,e,f) percentage of active labels per vertex for scale 0, 1 and 2 (black 0%, white 100%).

#### B.1.2 Venus

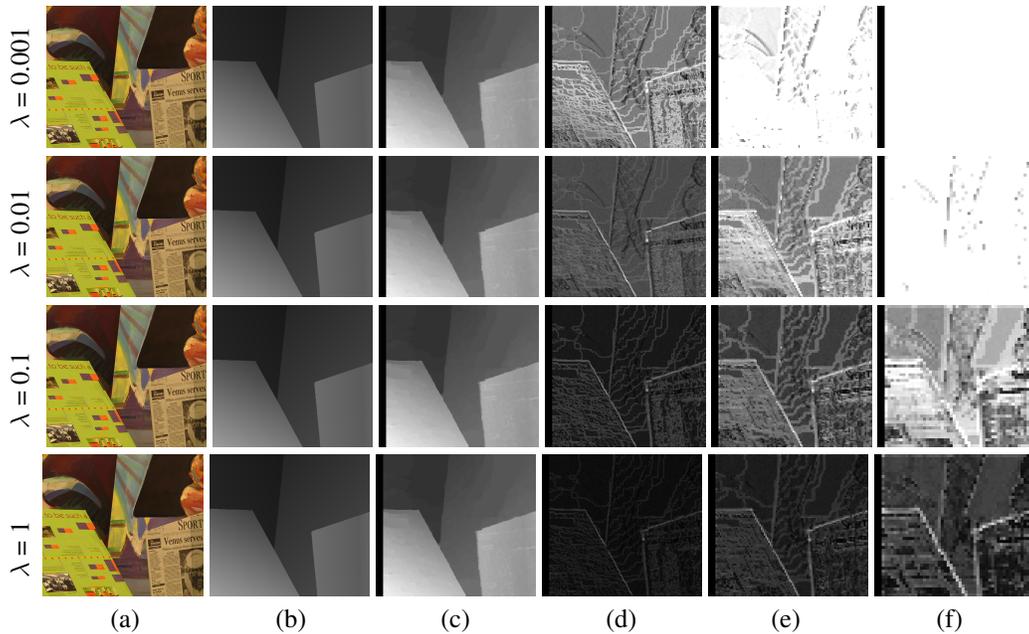


Figure 3: Results of our Inference by Learning framework for Venus. Each row is a different pruning aggressiveness value ( $\lambda$ ). (a) original image, (b) ground truth, (c) solution of the pruning framework, (d,e,f) percentage of active labels per vertex for scale 0, 1 and 2 (black 0%, white 100%).

### B.1.3 Teddy

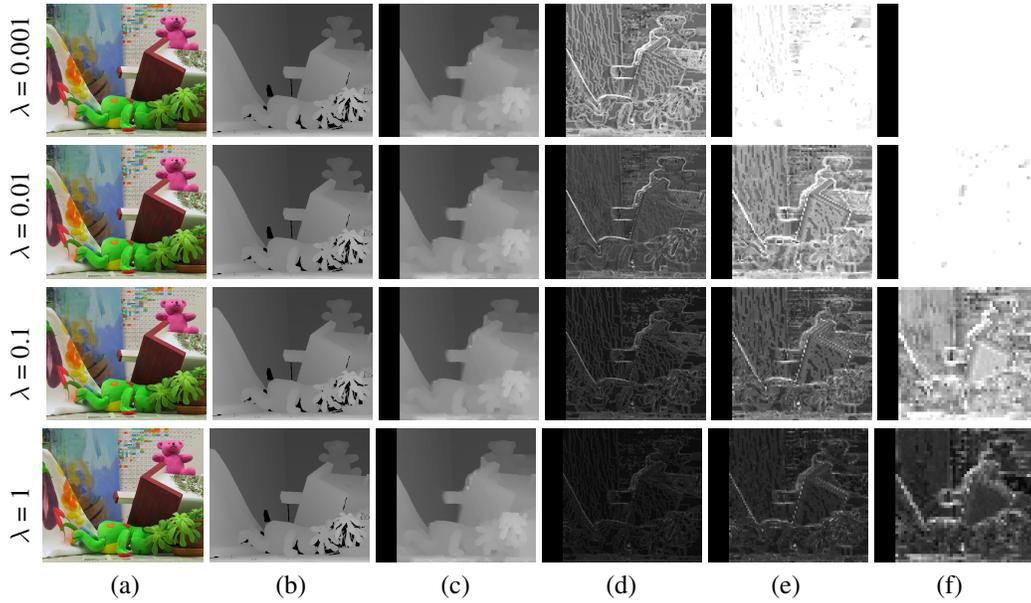


Figure 4: Results of our Inference by Learning framework for Teddy. Each row is a different pruning aggressiveness value ( $\lambda$ ). (a) original image, (b) ground truth, (c) solution of the pruning framework, (d,e,f) percentage of active labels per vertex for scale 0, 1 and 2 (black 0%, white 100%).

## B.2 Optical-Flow

### B.2.1 Army

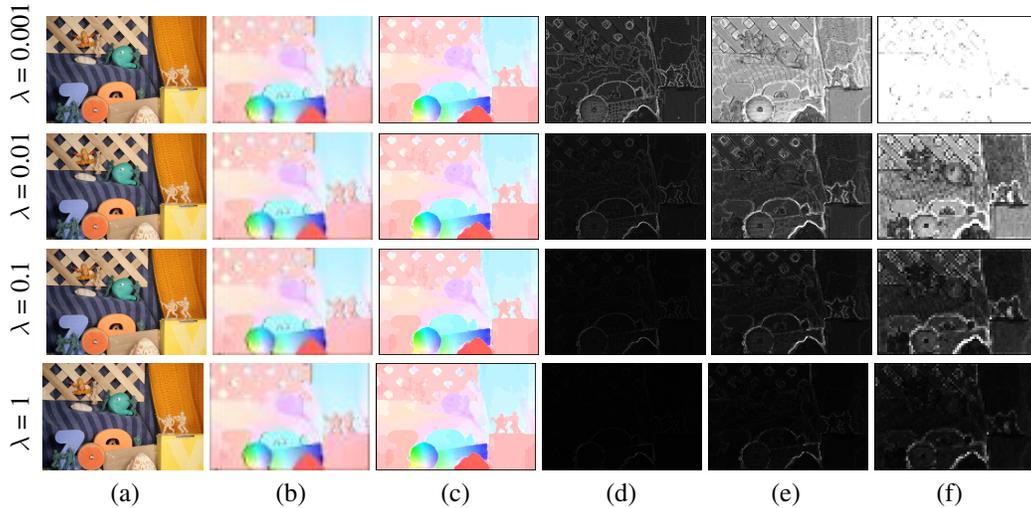


Figure 5: Results of our Inference by Learning framework for Army. Each row is a different pruning aggressiveness value ( $\lambda$ ). (a) original image, (b) ground truth, (c) solution of the pruning framework, (d,e,f) percentage of active labels per vertex for scale 0, 1 and 2 (black 0%, white 100%).

### B.2.2 Dimetrodon

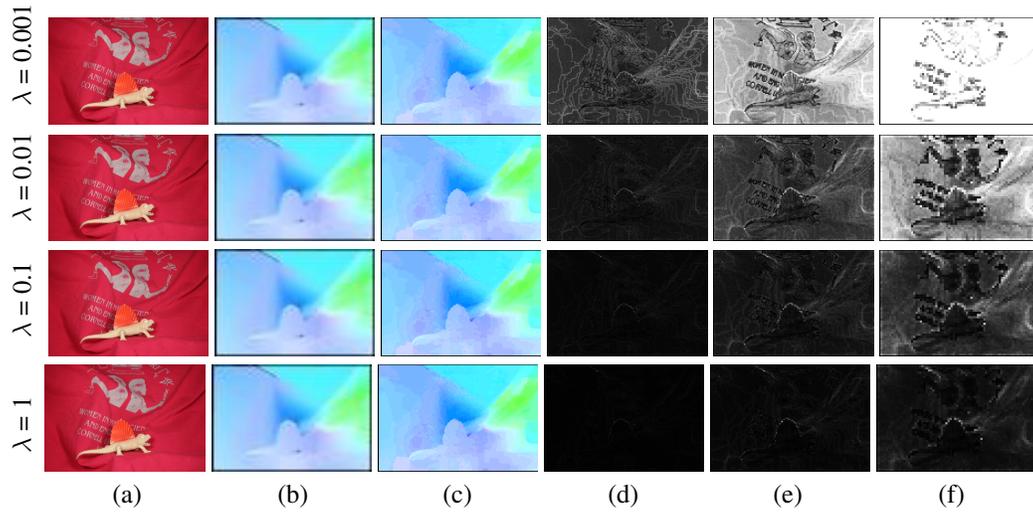


Figure 6: Results of our Inference by Learning framework for Dimetrodon. Each row is a different pruning aggressiveness value ( $\lambda$ ). (a) original image, (b) ground truth, (c) solution of the pruning framework, (d,e,f) percentage of active labels per vertex for scale 0, 1 and 2 (black 0%, white 100%).

### B.2.3 Rubberwhale

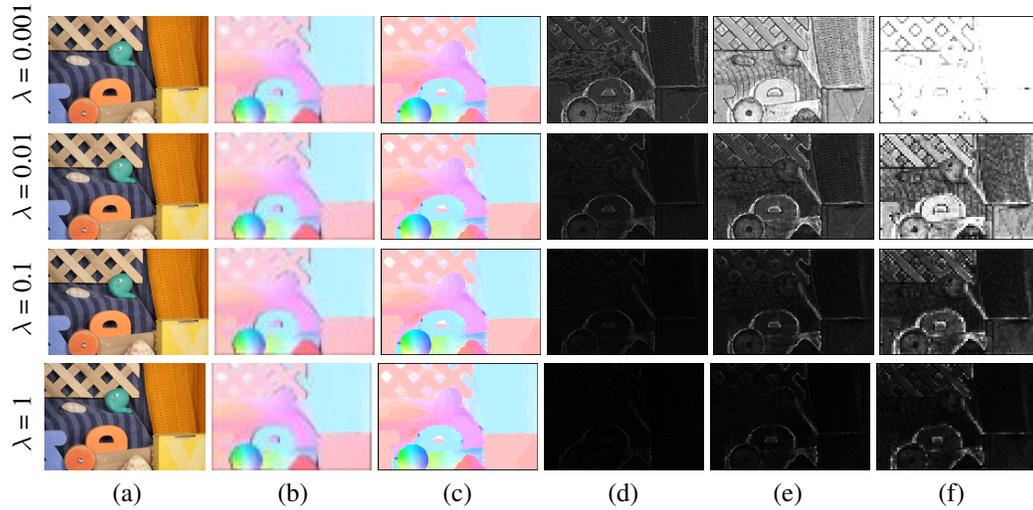


Figure 7: Results of our Inference by Learning framework for Rubberwhale. Each row is a different pruning aggressiveness value ( $\lambda$ ). (a) original image, (b) ground truth, (c) solution of the pruning framework, (d,e,f) percentage of active labels per vertex for scale 0, 1 and 2 (black 0%, white 100%).

### B.3 Denoising

#### B.3.1 Penguin

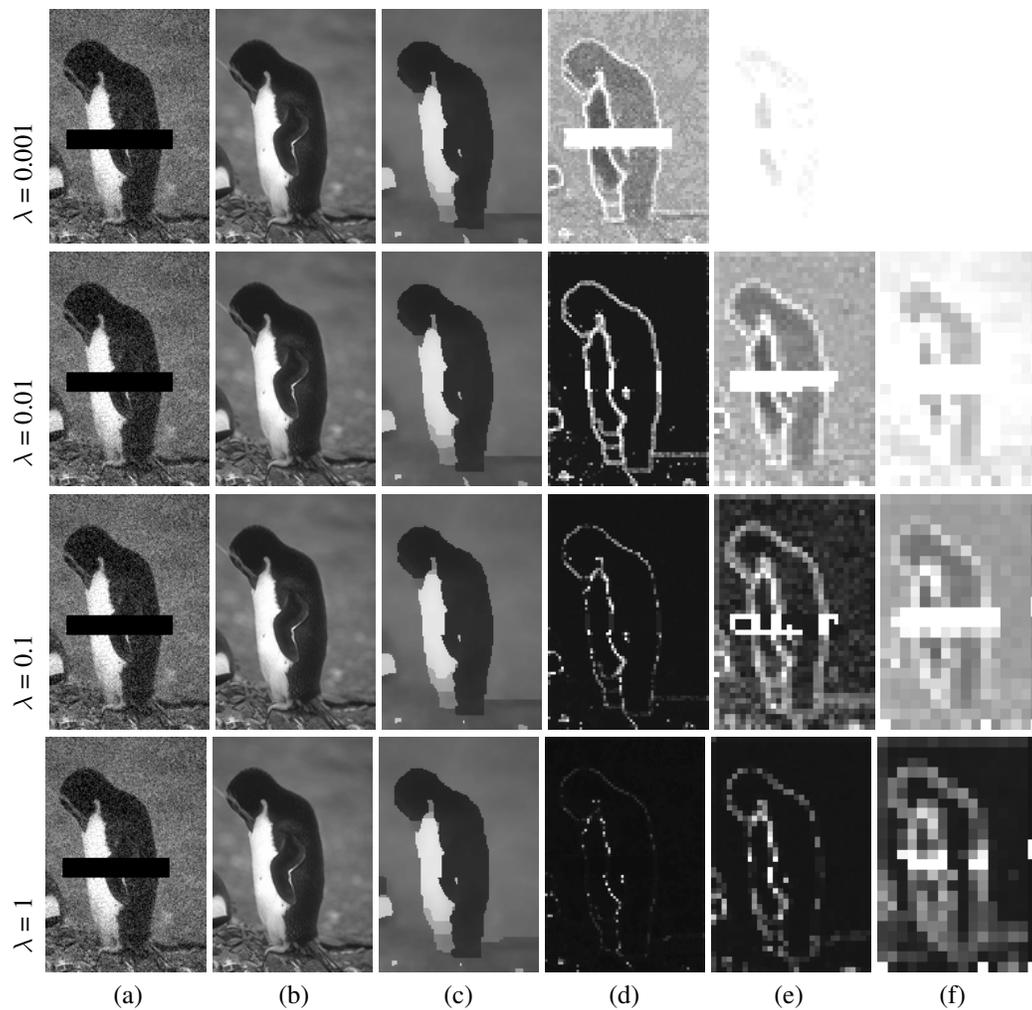


Figure 8: Results of our Inference by Learning framework for Penguin. Each row is a different pruning aggressiveness value ( $\lambda$ ). (a) original image, (b) ground truth, (c) solution of the pruning framework, (d,e,f) percentage of active labels per vertex for scale 0, 1 and 2 (black 0%, white 100%).

### B.3.2 House

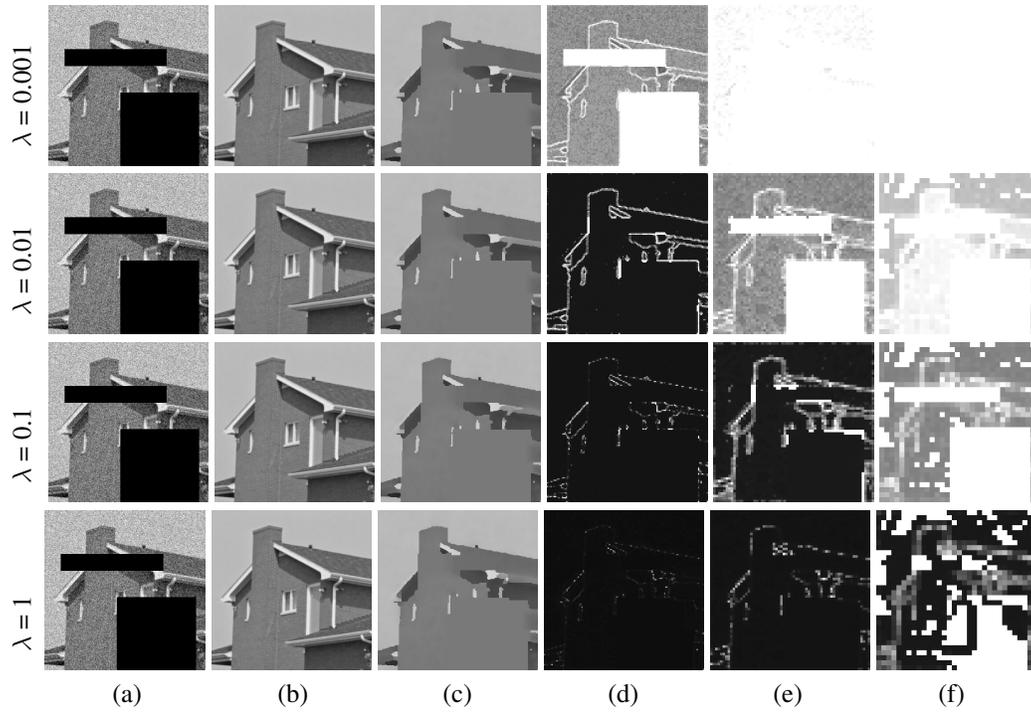


Figure 9: Results of our Inference by Learning framework for House. Each row is a different pruning aggressiveness value ( $\lambda$ ). (a) original image, (b) ground truth, (c) solution of the pruning framework, (d,e,f) percentage of active labels per vertex for scale 0, 1 and 2 (black 0%, white 100%).