

1 **General response to reviewers:** We thank the reviewers for their insightful and useful feedback! We are encouraged
2 that they believe our work "opens up many possibilities" (R3), and is "very novel" (R3), "promising" (R1), "simple yet
3 elegant" (R2) and "interesting" (R2, R3, R4). Reviewers appreciated that much prior work has involved hard-coding
4 levels of linguistic structure into different model architectures (R3) and that our method is a "general plug-and-play
5 model-agnostic method" (R4) that does not need to "decide on these points a priori" (R3).

6 **Larger points:** R4's primary concern is the gap between the performance of our BERT + prism model and SOTA
7 for the tasks we consider, and helpfully provides citations for SOTA models. However, the purpose of these experiments
8 is to consider how tools from spectral analysis can affect the representations of a single, general-purpose model (BERT)
9 across different tasks. This has both intrinsic scientific value as well as practical value, as these techniques could
10 then be integrated into the various task-specific architectures. Two other factors explain this gap: 1) BERT contextual
11 embeddings are known to perform surprisingly poorly on tasks beyond the word-level (see e.g. [2], where BERT
12 embeddings perform up to 16 points worse than even GloVe embeddings) 2) SOTA models are trained end-to-end,
13 while we train only a logistic regression on top of the token-level BERT embeddings without scale-specific pooling.

14 **Other points:** R1: "The authors do not fully describe the various hypotheses they imply..." This is a great
15 point, and we'll make sure points 2(a), (b), and (c) that R1 mentions are made explicit in the next revision.

16 **R2: Prism layer transforms are fixed; how does this compare to a learned transform?** This is an interesting
17 question. When pretraining with the prism layer, a fixed transform is useful because the MLM task is very local (Fig. 4)
18 and the fixed bands encourage the model to produce multiscale representations. Learning the transform to optimize the
19 MLM task may lead to all the frequency bands becoming local. However, it is an interesting direction for future work
20 whether clever regularization can get the best of both worlds here.

21 **R2: "In fig.5, why is BERT+prism worse for indices outside [200, 300]?"** We touch on this in L195-198, but the
22 higher loss around the masked region suggests that the model relies more on the (redacted) distant context than BERT
23 does to perform the MLM task, as we'd expect given the prism constraint.

24 **R3: "precise choice on where to use the prism layer raises some questions..."** We agree that it would be very
25 interesting to explore other ways of using the prism layer, including between every layer. We will include a comparison
26 to this setting for the camera ready.

27 **R3: "The way of dividing the embeddings into 5 sectors seems a bit naive"** We made this choice primarily to
28 enable clear comparisons between tasks at different linguistic scales. In practice, one could choose particular scales
29 relevant to desired end tasks or smoothly shift the frequency band between individual neurons as opposed to sectors of
30 neurons. We will note this in the paper, and that there is opportunity for future work!

31 **R4: "It would be nice to see ablations where you use high filters on POS tagging and low filters on para-**
32 **graph/document classification to see the gains that come from choosing the right set of filters for each task."** We
33 thank R4 for the useful suggestion. For the lowest frequency sector of the BERT + prism model, topic classification
34 accuracy is 45.1% (vs 51.0 for the full model and 5.3% for the highest-frequency sector). With the highest-frequency
35 sector, POS tagging accuracy is 84.1% (vs 94.4 for the full model and 16.8% for the lowest-frequency sector). This
36 suggests that the bands are largely but not entirely responsible for the high performance of BERT + prism, as expected.

37 **R4: "As a sanity check, you could try to see what happens if you don't finetune the initial BERT model on**
38 **wikitext-103?"** We thank R4 for the useful suggestion. The original BERT model achieves an accuracy of 94.6% for
39 POS tagging, 41.8 for dialog acts, 28.9 for topic classification, slightly worse than our model that was trained longer on
40 WikiText-103 (95.9%, 47.1%, 32.2% respectively). As before, these are trained on contextualized token representations
41 and are not comparable to models that perform pooling or are trained end-to-end. We will include this ablation in the
42 next revision.

43 **R4: "Since Figure 5 demonstrates good performance on long range masked language modeling, LAMBADA**
44 **might be a good benchmark to validate this."** This is an interesting idea for future work, as it is not yet straightforward
45 to use BERT for assigning probabilities to multi-token words in LAMBADA given 1) the constraints of the masked
46 language modeling interface and 2) that LAMBADA lacks end of sentence punctuation needed for bidirectional
47 conditioning.

48 Reviewers also offered a number of other suggestions which we are grateful for and will incorporate into the final
49 version of our paper.

50 **References:** [1] Understanding intermediate layers using linear classifier probes [2] Sentence-BERT: Sentence
51 Embeddings using Siamese BERT-Networks