

1 We are grateful to the anonymous referees for their valuable comments and suggestions. We acknowledge that all
2 referees correctly identified the main contributions of this work, namely: 1) a physically-inspired RNN generalising
3 LISTA-like networks to acoustic imaging and related spherical array signal processing tasks; 2) a physically-inspired
4 initialisation scheme for robust network training, supported by theoretical arguments; 3) a network architecture capable
5 of handling complex-valued microphone outputs and with parameter size growing linearly with the pixel resolution.
6 We address the comments of the reviewers below, denoted for brevity as **R1**, **R2**, **R3** respectively. Cited reference
7 numbers correspond to those in the bibliography of the main paper.

8 **(R1.1)** *A smoother introduction of equation (2) would be nice.* **(R2.1)** *The paper might need to provide more back-*
9 *ground info on acoustic imaging.* Equation (2) is based on the well-known point-source data-model in far-field array
10 signal processing, described in [52, Section 5.1] as well as [26]. The sparse imaging problem in [52, Section 5.6]
11 is moreover very similar to (2). However, for completeness and as per the referees' advice, we shall include a brief
12 derivation of (2) in the supplementary material of the final submission.

13 **(R1.2)** *PGD interpretation of the LISTA network is lost in practice when the ReLu activations are replaced by tanh.*
14 To retain the PGD interpretation of the network, one can use truncated ReLus as activation functions. Given the chosen
15 initialisation strategy, we will still converge with similar step sizes to those used with tanh non-linearities.

16 **(R1.3)** *I am surprised that 2760 data points were enough for training (without overfitting) and assessing the 5-*
17 *layered network.* For this experiment the spherical maps have resolution $N = 2234$. As a result, the APGD images
18 in the training set have total size $(2760 \times 0.8) \times 2234 = 4'932'672$. The total number of parameters in the 5-layered
19 recurrent architecture is $23(K) + 2234(\dim(\boldsymbol{\tau})) + 2234 \times 48(\dim(\mathbf{B})) = 109'489$. There is hence 45 times more data
20 than parameters to train, which is sufficient for the specific videoconference setup investigated to avoid overfitting.
21 Indeed, as revealed by the analysis of algorithm 2, the training only affects parameters in \mathbf{B} and $\boldsymbol{\tau}$ which correspond to
22 directions of nonzero intensity in the APGD ground truth images. Since source positions are in this case constrained to
23 a few latitude/longitude pairs, this reduces further the total number of parameters to train. In more complex setups,
24 where sources are unconstrained in location, the training set would of course need to be larger to avoid overfitting. Such
25 a setup was investigated in appendix G where the training set was composed of 16'000 images.

26 **(R1.4)** *I believe that the experimental results section could have been larger, with more results to support the claims.*
27 The ninth page will comment further on the experimental results. Furthermore, we will perform additional real-data
28 experiments using a new comprehensive dataset, better suited for data-augmentation. See also answer **(R3.1)**.

29 **(R1.5)** *Some confidence measure of the [runtime, resolution, contrast] scores could be useful to interpret the results.*
30 As per array signal processing standards, resolution was measured as the spread of the network impulse-response (see
31 fig. F.3), obtained with synthetic data from a single source. The contrast and runtime scores were computed for the
32 specific images shown in fig. 3 and fig. F.4. The final submission will provide average scores over the entire test set with
33 confidence measures. For example, the average contrast scores in the videoconference setup are $0.99 (\pm 0.0081)$ and
34 $0.89 (\pm 0.07)$ for DeepWave and DAS respectively (corresponding to a contrast improvement between 2 and 22%).

35 **(R2.2)** *The network was [tailored to] acoustic imaging, and not designed for a wider range of applications.* The
36 focus on acoustic imaging stems from its importance in industrial applications, notably smart speaker assistants.
37 However, equation (2) is based on a generic physical model common to many far-field array signal processing problems,
38 including radar, sonar, interferometry, fault detection and medical imagery [26]. Since the submission, DeepWave
39 has been successfully tested in the context of radio astronomy with no architectural modifications. In addition, we
40 stress that DeepWave is *not* restricted to spherical arrays. This assumption only motivates our initialisation scheme via
41 proposition 1. As a matter of fact, the array used in fig. 3f is a tetrahedron.

42 **(R2.3)** *Is it possible to compare with the performance of LISTA?* We tried and this is not possible for the following
43 reasons: 1) training proved impossible using the LISTA parametrisation (memory overflow even with sparsification as
44 in [16]) and random initialisation; 2) without the Khatri-Rao parametrisation, the network output is not guaranteed to be
45 real-valued given complex-valued raw microphone correlations.

46 **(R3.1)** *I cannot find out any ablation study of the parameters of the proposed method.* An ablation study has been
47 conducted but left out of the manuscript due to space constraints. More specifically, we froze the training of network
48 parameters, fixing them to their initial values provided in (10). All 6 combinations of free/frozen shrinkage, deblurring
49 and backprojection operators were investigated. We also investigated the effect of the associated parameter regularisation
50 terms in (9). We noticed that the shrinkage operator $\boldsymbol{\tau}$ was most affected by regularisation and training. This is because
51 the deblurring and backprojection operators are, for the specific experimental conditions investigated (point sources,
52 anechoic chambre, near-spherical geometries), very well modelled by our initialisation scheme (10). For more complex
53 environments and array geometries, the conclusions of the ablation study may however differ significantly. These results
54 will be reported in the supplementary material of the final manuscript.

55 **(R3.2)** *I cannot find out any quantitative comparison of the proposed method with state-of-the-art methods.* Quan-
56 titative results in terms of runtime, resolution and contrast were provided for DeepWave and the state-of-the-art DAS
57 algorithm for each experiment. We refer moreover the reviewer to **(R1.5)** regarding confidence measures on the scores.

58 **(R3.3)** *Stylistic comments.* We welcome these remarks and will take them into account for the final submission, while
59 abiding with NeurIPS official stylistic guidelines.