

1 We greatly appreciate the three reviewers for their valuable comments. The following are our responses. We will add
2 the following results and discussions in the final version of the manuscript.

3 **[RESPONSE TO REVIEWER #1]** (1) To evaluate the performances based on a metric other than the log-
4 likelihood, we newly carried out the time prediction experiments; we predict the time t_{i+1} of the next event from the
5 times of the preceding events. We herein use the median t_{i+1}^* of the predictive distribution to predict t_{i+1} for each
6 model. To obtain the median t_{i+1}^* , we use the relation $\Phi(t_{i+1}^* - t_i | \mathbf{h}_i) = \log(2)$, where Φ is a cumulative hazard
7 function. This relation is derived from the property that the integral of the intensity function over $[t_i, t_{i+1}]$ follows
8 the exponential distribution with mean 1. Then, the median t_{i+1}^* can be efficiently obtained by solving the relation
9 using a root finding method (e.g., bisection method); it takes only a second for our model to generate predictions for
10 20000 events. Therefore, the cumulative hazard function also plays a crucial role in generating a median predictor.
11 The performance is evaluated by the mean absolute error, summarized below. In the table, the best score is in bold,
12 and it is in red if the difference between the best score and the second best score is statistically significant ($p < 0.01$).

	S-Poisson	N-Poisson	S-Renewal	N-Renewal	SC	Hakes1	Hawkes2	Finance	Call	Meme	Music	AVERAGE
constant	0.696	0.704	1.085	0.450	0.543	0.915	1.075	0.883	0.966	0.848	1.066	0.839
exponential	0.696	0.716	0.917	0.452	0.498	0.854	0.986	0.840	0.922	0.823	0.788	0.772
piecewise const.	0.696	0.716	0.982	0.437	0.494	0.850	0.965	0.839	0.878	0.826	0.856	0.776
neural network	0.696	0.710	0.894	0.414	0.496	0.848	0.962	0.847	0.873	0.811	0.783	0.758

15 We find that our model performs better than the other models on average and that the performance of our model is best
16 or close to the best for the most cases. These results demonstrate the effectiveness of our model in the prediction task.

17 **[RESPONSE TO REVIEWER #2]** (2) We recognized the importance of the CT-LSTM model [7] in the current
18 context, and we will discuss more on it in the final version of the manuscript. We newly compared the performances
19 between our model and the CT-LSTM model. The performance is evaluated in terms of the negative log-likelihood per
20 event calculated for the test data. The following table lists the scores of the CT-LSTM model relative to our model; the
21 positive score means that our model is better than CT-LSTM model. In the table, the score is in blue if the difference
22 between the two models is statistically significant ($p < 0.01$).

	S-Poisson	N-Poisson	S-Renewal	N-Renewal	SC	Hakes1	hawkes2	Finance	Call	Meme	Music	AVERAGE
CT-LSTM	-0.002	-0.013	0.012	-0.007	-0.008	-0.002	0.002	-0.011	0.060	0.590	0.163	0.071

24 We find that our model performs much better than the CT-LSTM model for the Meme and Music datasets and that
25 the performances are very close to each other for the other cases. Accordingly our model performs better than the
26 CT-LSTM model on average. We also evaluated the predictive performances in terms of the mean absolute error. The
27 average error over all the datasets is 0.766 for the CT-LSTM model and 0.758 for our model, and the difference is
28 statistically significant ($p < 0.01$). These results indicate the superior performance of our model.

29 The technical advantage of our model is that the cumulative intensity function is directly modeled by a neural network,
30 which makes the estimation and prediction efficient, and our model is also relatively easy to implement. For the
31 CT-LSTM model, the intensity function is modeled as a nonlinear function of the time-evolving memory cells, and
32 the estimation and prediction are simulation-based, which can be computationally expensive and can deteriorate the
33 performance.

34 (3) The exponential model cannot fit to the Hawkes1 model perfectly because the hazard functions are slightly different
35 from each other. While the hazard function of the exponential model is an exponential function, that of the Hawkes1
36 model is the sum of an exponential function and a constant μ (see line 211).

37 **[RESPONSE TO REVIEWER #3]** (4) A method to derive an intensity function is described in detail in the
38 original submission (please see lines 134-140 in the manuscript and lines 3-20 in the supplementary text).

39 (5) In *RESPONSE TO REVIEWER #1*, we described an efficient method to make a median prediction based on the
40 cumulative hazard function, and we additionally evaluated the predictive performances based on the mean absolute
41 error, which finally showed the effectiveness of our model.

42 (6) The reviewer #3 commented that "*The proposed model is mainly based on monotonic networks and technical
43 novelty is a bit incremental ...*". However, the novelty of our study is, we believe, rather that our approach enables
44 us to model an intensity function in a flexible way and to exactly and efficiently compute the log-likelihood, which is
45 important for application. The monotonic network is just a component of our new approach. This method is clearly
46 advantageous against the studies that use a parametric hazard function or the studies [6, 7] that rely on numerical
47 approximations to evaluate a model with a flexible intensity function, which can be computationally expensive and can
48 deteriorate the performance. Our study therefore demonstrates the effectiveness of a neural network for the modeling
49 of point processes. We hope that this point is positively evaluated.